



2020 Year 11 Mathematics Specialist

Mr Daniel Comtesse

Semester Two Examination, 2020

Mandurah Catholic College

Question/Answer booklet

daniel.comtesse@cewa.edu.au

**Section One:
Calculator-free**

Student Name: _____

School: _____

Time allowed for this section

Reading time before commencing work: five minutes
Working time: fifty minutes

Materials required/recommended for this section

To be provided by the supervisor

This Question/Answer booklet
Formula sheet

To be provided by the candidate

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener, correction fluid/tape, eraser, ruler, highlighters

Special items: nil.

Important note to candidates

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised material. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

Exams are to be returned to the ViSN teacher by the ViSN mentor (scan completed assessment and email to teacher above) on the day of the exam.

Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of examination
Section One: Calculator-free	8	8	50	52	35
Section Two: Calculator-assumed	13	13	100	98	65
Total					100

Instructions to candidates

- The rules for the conduct of examinations are detailed in the school handbook. Sitting this examination implies that you agree to abide by these rules.
- Write your answers in this Question/Answer booklet preferably using a blue/black pen. Do not use erasable or gel pens.
- You must be careful to confine your answers to the specific question asked and to follow any instructions that are specific to a particular question.
- Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
- It is recommended that you do not use pencil, except in diagrams.
- Supplementary pages for planning/continuing your answers to questions are provided at the end of this Question/Answer booklet. If you use these pages to continue an answer, indicate at the original answer where the answer is continued, i.e. give the page number.
- The Formula sheet is not to be handed in with your Question/Answer booklet.

Markers use only		
Question	Maximum	Mark
1	7	
2	6	
3	8	
4	7	
5	5	
6	6	
7	7	
8	6	
S1 Total	52	
Total	100%	

Section One: Calculator-free**35% (52 Marks)**

This section has **eight** questions. Answer **all** questions. Write your answers in the spaces provided.

Working time: 50 minutes.

Question 1**(7 marks)**

Two matrices are $A = \begin{bmatrix} -2 & 2 \\ -4 & 3 \end{bmatrix}$ and $B = \begin{bmatrix} 0 & -5 \\ 10 & 5 \end{bmatrix}$. Determine

(a) $3A - 2B$.

(2 marks)

(b) A^{-1} .

(2 marks)

(c) $AB + B^2$.

(3 marks)

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Question 2

(6 marks)

(a) State the exact value of $\cot 60^\circ$.

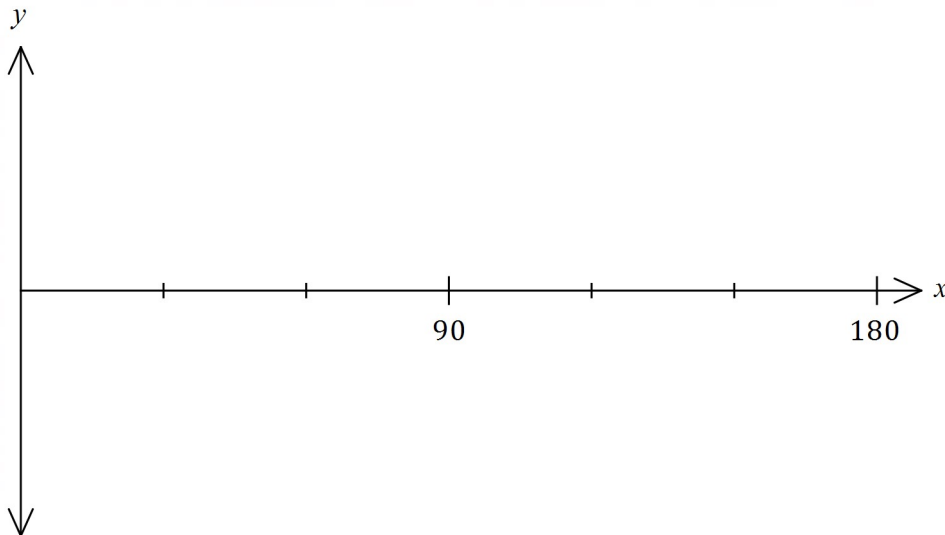
(1 mark)

(b) Given that $\sec \theta = \frac{3}{2}$ and $-90^\circ \leq \theta \leq 0^\circ$, state the exact value of $\operatorname{cosec} \theta$.

(2 marks)

(c) Sketch the graph of $y = 2 \sec x$ for $0^\circ \leq x \leq 180^\circ$ on the axes below.

(3 marks)



Question 3

(8 marks)

(a) Express $(\sqrt{5} + \sqrt{-5})^2$ in the form $a + bi$ where $a, b \in \mathbb{R}$.

(2 marks)

(b) Two complex numbers are $u = 8 + i$ and $v = 2 - i$. Calculate

(i) $u \times v$.

(1 mark)

(ii) $u \div v$.

(2 marks)

(iii) $\text{Im}(2\bar{v} - iu)$.

(3 marks)

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Question 4

(7 marks)

- (a) Use an angle sum identity to prove that $\tan 2A = \frac{2 \tan A}{1 - \tan^2 A}$. (2 marks)

- (b) Hence, or otherwise, prove that $\tan 3A = \frac{3 \tan A - \tan^3 A}{1 - 3 \tan^2 A}$. (3 marks)

- (c) Solve $3 \tan A - \tan^3 A = 1 - 3 \tan^2 A$ for $0^\circ < A < 30^\circ$. (2 marks)

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Question 5**(5 marks)**

AC is a diameter of a circle centre O and point B lies on the circumference of the circle.

Let $\overrightarrow{OA} = \mathbf{a}$ and $\overrightarrow{OB} = \mathbf{b}$.

Use a vector method to prove that $\angle ABC = 90^\circ$.

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Question 6

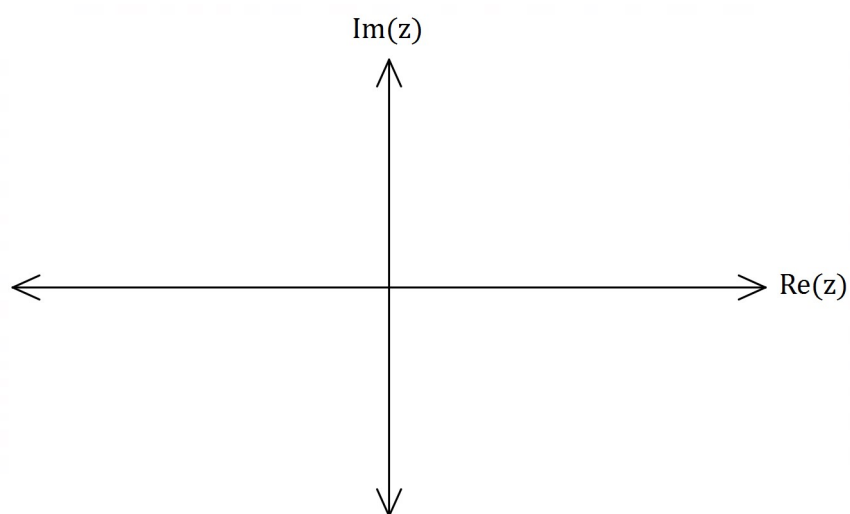
(6 marks)

- (a) Determine the equation of the real quadratic $f(z)$ in the form $z^2 + az + b$ given that $f(5 - 3i) = 0$. (2 marks)

(b) Let $g(z) = z^2 - 8z + 17$.

- (i) Determine z_1 and z_2 , the complex roots of g . (2 marks)

- (ii) Sketch and label z_1 , z_2 and $w = z_1 + z_2$ in the complex plane below. (2 marks)



Question 7**(7 marks)**

Use mathematical induction to prove the following proposition $P(n)$ for every integer $n \geq 0$.

$$P(n): 1 + 9 + 17 + 25 + \dots + (8n + 1) = (n + 1)(4n + 1)$$

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Question 8

(6 marks)

(a) Determine the vector projection of $2\mathbf{i} - \mathbf{j}$ on $-3\mathbf{i} + 4\mathbf{j}$. (2 marks)

(b) The vectors $a\mathbf{i} + \mathbf{j}$ and $4\mathbf{i} + b\mathbf{j}$ are perpendicular and the sum of their magnitudes is 10. Determine the values of the constants a and b . (4 marks)

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Supplementary page

Question number: _____

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